

Unit-2 (Nuclear Physics)

① Nuclear reaction

(*) Write down the quantities which are conserved in nuclear reaction?

→ (i) The mass no. should be conserved and proton no. should be conserved.

(ii) Momentum should be conserved.

(iii) Mass - Energy should be conserved.

(iv) Charge should be conserved

(*) What do you mean by

(i) Nuclear reaction?

(ii) what is endothermic and exothermic

Nuclear reaction?

→ (i) The amount of energy released in a nuclear reaction, is known as Q-value of nuclear reaction.

If Energy is absorb in a nuclear reaction, then it is known as endothermic reaction.

The Q-value is negative in this case.

If Energy is release in a nuclear reaction, then it is known as Exothermic reaction.

The Q-value is +ve in this case.

(7) Yield = % of product / % of reactant.

⑩ Find the expression for Q-value in terms of mass of the reactants, mass of the product. Hence find the expression for Q-value in terms of Binding energy of Product and reactant?



Reactant → Product.

Here, M_x = Rest mass of nucleus "x".

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My first visit to the city.

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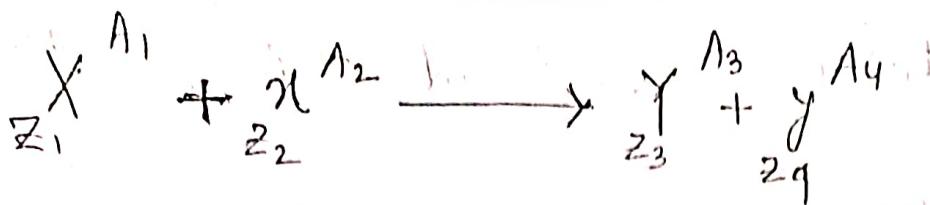
Using Mass-Energy conservation,

$$M_{x_1}c^2 + T_x + m_x c^2 + T_x = M_y c^2 + T_y + m_y c^2 + T_y$$

$$\Rightarrow (T_Y + T_y) - (T_x + T_z) = (M_X + m_x) c^2 \quad T_x = KE \text{ of nucleus } x$$

1. $(x^2 + y^2)^{1/2} = 1$ $\Rightarrow x^2 + y^2 = 1$ \Rightarrow $x^2 = 1 - y^2$

$$2) Q\text{-value} = \frac{(\text{Mass of reactant} - \text{Mass of product})c}{\text{Mass of reactant}}$$



$$A_1 + A_2 = A_3 + A_4$$

$$Z_1 + Z_2 = Z_3 + Z_4$$

$$\text{B.E. of } X = \left\{ Z_1 m_p + (A_1 - Z_1) m_n - M_x \right\} c^2$$

$$\text{B.E. of } Y = \left\{ Z_2 m_p + (A_2 - Z_2) m_n - M_y \right\} c^2$$

$$\text{B.E. of } Z = \left\{ Z_3 m_p + (A_3 - Z_3) m_n - M_z \right\} c^2$$

$$\text{B.E. of } W = \left\{ Z_4 m_p + (A_4 - Z_4) m_n - M_w \right\} c^2$$

\therefore B.E. Product - B.E. of Reactant.

$$= \text{B.E. of } Y + \text{B.E. of } Z - \text{B.E. of } X$$

$$- \text{B.E. of } W$$

$$= \left[(Z_3 + Z_4) m_p + (A_3 + A_4 - Z_3 - Z_4) m_n \right] c^2$$

$$= -M_y - M_w - (Z_1 + Z_2) m_p$$

$$- (A_1 + A_2 - Z_1 - Z_2) m_n$$

$$+ M_n + m_n$$

$$= \left[0 \cdot m_p + 0 \cdot m_n + M_n + m_n - [M_y + M_w] \right] c^2$$

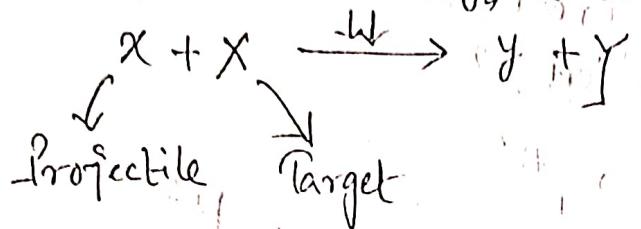
$$= (M_n + m_n) c^2 - (M_y + M_w) c^2$$

$$\therefore Q\text{-value} = \boxed{\text{B.E. Product} - \text{B.E. Reactant}}$$

④ what do you mean by threshold KE?

→ the minimum KE of projectile required in endothermic nuclear reaction is known as threshold Kinetic Energy.

for example - energy absorbed (endothermic reaction)



let, the mass of the nuclei 'X' = M_X

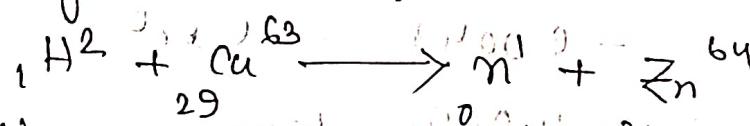
" " " for particle 'Y' = m_Y

the threshold KE, in this case -

$$K_{th} = -Q \left(1 + \frac{m_Y}{M_X}\right), \quad Q \in Q\text{-value.}$$

of the
nuclear
reaction.

⑤ calculate, the Q -value of the following reaction?



$$M(H^2) = 2.014102 \text{ amu}, \quad M({}_{29}^{63}Cu) = 62.929599 \text{ amu}$$

$$M(n) = 1.008665 \text{ amu.}$$

If the KE of H^2 is 12 Mev in collision cu at rest,
the KE of n is 16.85 Mev. Find the KE of Zn .

$$\begin{aligned} Q &= \left[0.005894 \right] \text{ amu} \times c^2 \\ &= 5.499102 \text{ Mev.} \end{aligned}$$

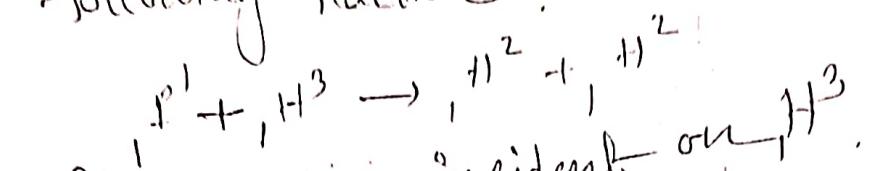
$$1 \text{ amu} = 931 \text{ Mev}$$

Again, Q value = KE of Product - KE of reactants

$$\Rightarrow S. \text{ (199102)} = 16.85 + KE_{2n} - 12$$

$$\Rightarrow KE_{2n} = 0.649102 \text{ MeV.}$$

(*) calculate the threshold KE (in MeV) for the following reaction?



(i) if the proton incident on H^3 .

(ii) if the H^3

$$M(p^1) = 1.007825 \text{ amu}, \quad M(H^3) = 3.016049 \text{ amu}$$

$$M(H^2) = 2.014102 \text{ amu}$$

$$\Rightarrow Q = (4.028204 + 4.023874) \text{ amu} \times c^2$$

$$= 0.00433 \text{ amu} \times c^2$$

$$= 4.03989 \text{ MeV.}$$

$$(i) K_{th} = 4.03989 \left(1 + 0.334154 \right)$$

$$= 5.38983 \text{ MeV.}$$

$$(ii) K_{th} = 4.03989 \left(1 + 2.992542 \right)$$

$$= 16.129432 \text{ MeV.}$$

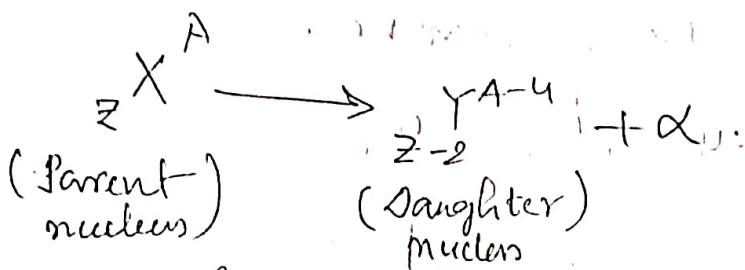
α -Particle

Q) Find and expression for Q-value in α -disintegration of nucleus θ

ii) S.T in α -disintegration Maximum

Energy of the reaction is carried out by
-the α - particle?

→ (i) We consider a nucleus X emit's an α -Particle from rest ..



The mass of the nucleus $X = M_X$ and the mass of the nucleus α -particle $= M_\alpha$

the Q-Value of the reaction

$Q = KE \text{ of product} - KE \text{ of reactant}$

$$= \frac{1}{2} M_1 V_1^2 + \frac{1}{2} M_2 V_2^2 - 0 \quad \left| \begin{array}{l} V_Y = \text{Velocity} \\ \text{of} \\ \text{Nucleon} \end{array} \right.$$

$$= \frac{1}{2} M_y V_y + \frac{1}{2} M_x V_x \rightarrow ①$$

$V_x = \text{Velocity}$
 at

Curing Momentum Conservation

$$O = M_x v_x + M_y v_y$$

$$\therefore V_F = \frac{-M \alpha^N \alpha}{1 - \mu}$$

Using (11) in (1).

$$Q = \frac{1}{2} M_p \frac{M_\alpha^2 v_\alpha^2}{M_\gamma^2} + \frac{1}{2} M_\alpha v_\alpha^2$$

$$= \frac{1}{2} M_\alpha V_\alpha^2 \left[1 - \frac{M_\alpha}{M_\gamma} \right]$$

$$\Rightarrow \frac{1}{2} M_\alpha V_\alpha^2 = \frac{Q}{1 - \frac{M_\alpha}{M_\gamma}}$$

$$\Rightarrow \text{KE of } \alpha\text{-Particle} = \frac{M_\gamma}{M_\alpha + M_\gamma} \cdot Q$$

Mass of nucleus & mass no.

$$M_\gamma = A - 4, M_\alpha = 4.$$

$$\therefore \boxed{\text{KE of } \alpha = \frac{A-4}{A} Q}$$

This is the expression for KE of α -particle emitted from a nucleus of mass no. A.

If $A \gg 4$, the maximum energy of α -disintegration is carried out by the α -particle.

(*) The Q-value of α -disintegration from $^{235}_{92}\text{U}$ is 12 Mev. Find the KE of α particle and Daughter nucleus!

$$\rightarrow Q = 12 \text{ Mev.}$$

$$\text{KE}_\alpha = \frac{231}{235} \times 12 = 112.795 \text{ Mev.}$$

$$\text{KE}_\gamma = \frac{4}{A} Q = \frac{4}{235} \times 12 \approx 0.204 \text{ Mev}$$

Q(i) what do you mean by range of α -Particle?

(ii) state the factor from which range of α -Particle ?

→ (i) the distance through which α -Particle travels in a specific medium before stopping to ionize the medium is known as range of α -Particle.

(ii) the range of α -Particle depends on following factor's —

① the initial energy of α -Particle :-

the greater the initial energy of α -Particle
the greater the range of α -Particle.

② Ionization Potential of the gas :-

the range of α -Particle is inversely proportional to ionization energy of the gas.

③ The range of α -Particle is inversely proportional to density of the medium.

④ With the increasing pressure, range of α -Particle decreases. with the increase of temp. the range of α -Particle increases.

* State and prove Geiger's law for the range of α -Particle?

→ According to Geiger's law the range of α -Particle is proportional to cube of initial velocity of α -Particle.

Ques. $R \propto V^3$: where,
 R = Range of α -particle

V = Initial velocity of
 α -particle

Proof

The decreasing KE of α -particle per unit length is inversely proportional to its velocity.

i.e., $\frac{dE}{dx} \propto -V$

$$\Rightarrow \frac{dE}{dx} = -\frac{q}{m} \frac{v}{V} ; E = \frac{1}{2}mv^2$$

$$\Rightarrow \frac{1}{2}m \cdot 2v \frac{dv}{dx} = -\frac{q}{m}$$

$$\Rightarrow v^2 dv = -\frac{q}{m} dx$$

Integrating both sides

$$\int_{v_0}^0 v^2 dv = -\frac{q}{m} \int_0^R dx$$

$$\Rightarrow \left[\frac{v^3}{3} \right]_{v_0}^0 = -\frac{q}{m} R$$

v_0 = initial velocity

R = Range of α -particle

$$\Rightarrow +\frac{V_0^3}{3} = +\frac{q}{m} R$$

$$\therefore \boxed{R \propto V_0^3}$$

This is known as Geiger's law.

(*) State Geiger-Nuttal Law for the range of α -Particle?

ii) Find the relation between Range of α -Particle and decay const. of radioactive nucleus?

(i) → Geiger and Nuttal showed that, the range of α -Particle in air medium and the disintegration const. of Parent nucleus from which α -Particle is emitted, is connected by a simple relation called Geiger-Nuttal law.

(ii) → the empirical expression of Geiger-Nuttal law,

$$\log_e \lambda = A + B \log_e R, \text{ where,}$$

λ = disintegration const.

again, $T_{1/2}$ (Half life) $\geq \frac{0.693}{\lambda}$

R = range of α -Particle

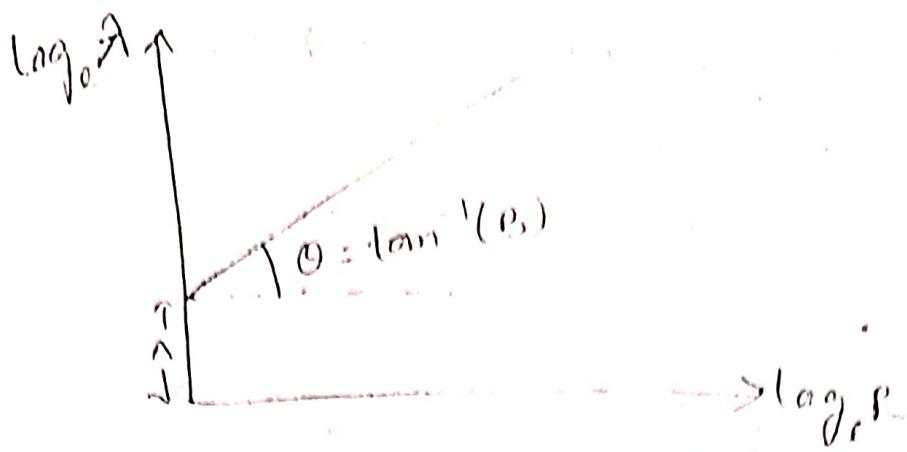
$$\Rightarrow \lambda = \frac{0.693}{T_{1/2}} \text{ in half life units.}$$

$$\log_e \left\{ \frac{0.693}{T_{1/2}} \right\} = A + B \log_e R$$

$$\Rightarrow \log_e \frac{0.693}{T_{1/2}} - \log_e R = A + B \log_e R.$$

$$\boxed{\Rightarrow -\log_e \frac{T_{1/2}}{R} = A + B \log_e R}$$

This is the relation between Range of α -Particle and the Half life of the nucleus from which the α -Particle was emitted.



(i) Find the Coulomb Potential of the nucleus $_{92}^{235}\text{U}$ (ii) Find the interaction energy, when a α -particle is emitted from the nucleus ?

$$\rightarrow \text{(i)} \text{ for } _{92}^{235}\text{U}, z = 92$$

Radius of the nucleus, $R = R_0 A^{1/3}$

$$R_0 = 1.3 \text{ fm}$$

$$R = 1.3 \times 10^{-15} (235)^{1/3} \text{ m}$$

Coulomb Potential on the surface of nucleus, $V = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{R}$

$$= 9 \times 10^9 \times \frac{92 \times 10^{-19} \times 1.6}{8.02 \times 10^{-15}} \text{ J/C}$$

$$= 165.187 \times 10^5 \text{ J/C}$$

(ii) The interaction Energy, when a α -particle is emitted from the nucleus of $_{92}^{235}\text{U}$

The interaction energy,

$$V = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{R}$$

$$= 9 \times 10^9 \times \frac{2e(2-2)e}{R}$$

$$= 9 \times 10^9 \times \frac{2 \times 90 \times (1.6) \times 10^{-38}}{1.8 \times 10^{-15}}$$

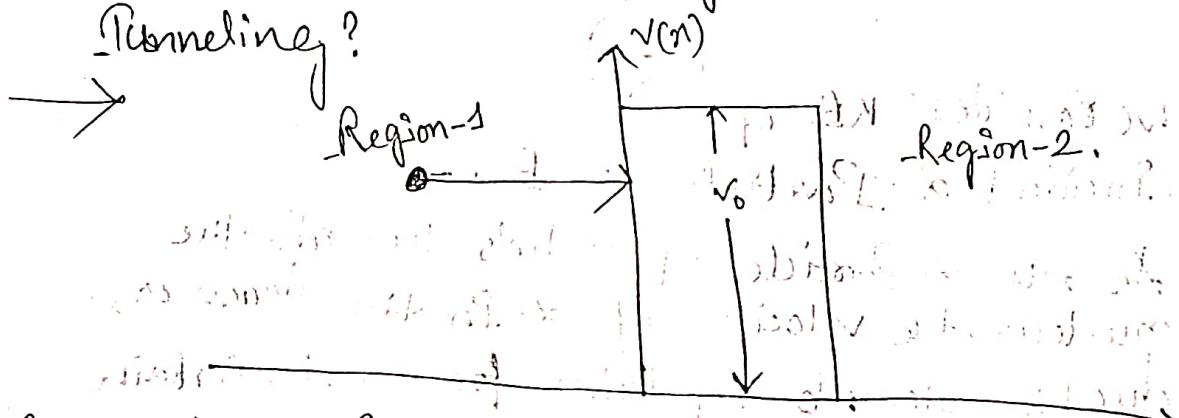
$$= 319.107 \times 10^{-14}$$

$$= 323.19 \times 10^5 \text{ eV}$$

$$= 32.319 \text{ MeV}$$

For the emission of α -particle, the KE of α -Particle must be greater than equal to 32.319 MeV theoretically.

④ What do you mean by Quantum mechanical Tunneling?



We consider a potential barrier of height V_0 , shown in the figure. And Particle with KE E incident on the Potential barrier.

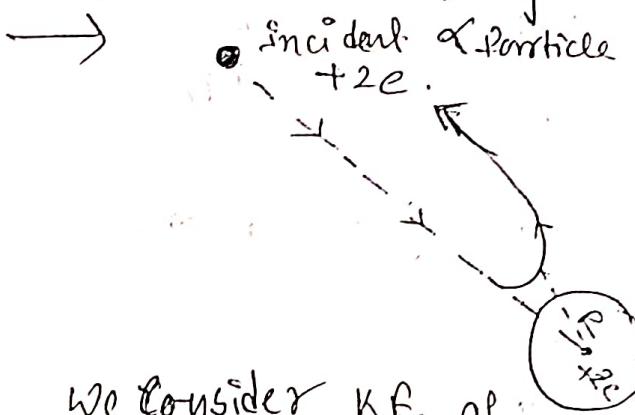
If $E < V_0$, then probability of particle to appear in region-2

after crossing the potential barrier.

But quantum mechanically, there is always a probability that, the particle will penetrate the potential barrier and appear in a region-2. This phenomenon is known as quantum mechanical tunnelling.

The emission of α -particle from the nucleus is a proper example of Quantum Mechanical tunneling.

⑧ Using Rutherford α -scattering experiment, find the radius of nucleus?



We consider KE of

Incident α -Particle = E.

As, the α -particle approaches toward's the nucleus, the velocity of α -particle decreases, due to coulomb repulsion force. At a certain point near the surface of nucleus, the velocity of α -particle is zero. As, electrostatic field is conservative, the total

Energy should be const.

$$E = \frac{1}{4\pi\epsilon_0} \cdot \frac{2e \cdot 2e}{R}$$

$$E = \frac{2ze^2}{4\pi\epsilon_0 R}$$

$$\Rightarrow R = \frac{2ze^2}{4\pi\epsilon_0 E}$$

R is nearly equal to the radius of the nucleus.

This is an approximate expression of radius of nucleus from Rutherford α -scattering experiment.

(*) Find the radius of gold nucleus if the KE of α -particle is 8-Mev, in Rutherford α -scattering expt?

$$\rightarrow R = \frac{2 \times 79 \times (1.6) \times 10^{-38}}{8 \times 10^6 \times 1.6 \times 10^{-19}} \times 9 \times 10^{-3}$$

$$= 284.4 \times 10^{-16} \text{ m}$$

$$= 28.44 \text{ fm.}$$

(k) → The distance through which α -particle travels in a specific medium before stopping to ionize the medium is known as Range of α -particle.

(2021)

(l) → A subatomic particle having the same mass as one of the particles of ordinary matter but opposite electric charge and magnetic moment.

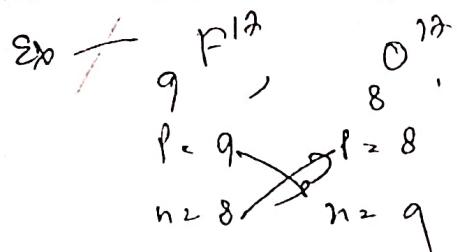
Ex - antiparticle of $e^- \rightarrow$ Positron ($+e$)

" " Proton \rightarrow antiproton ($-e$)

" " neutron \rightarrow antineutron (\bar{n})

(m) → The inverse process of β -decay is e^- capture, where, the nucleus absorbs one of its own orbital electrons if the absorption of electron from the K-shell then it's called K-capture.

(n) → The neutron no. of 1st nucleus is equal to proton no. of 2nd nucleus and neutron no. of 2nd nucleus is equal to the proton no. of 1st nucleus then the nuclei is known as mirror nuclei.



(o) → The reaction or rate is the no. of interacting taking place in one cubic centimeter per one second.

(f) \rightarrow Internal conversion is a non radioactive atomic decay process where an excited nucleus interacts electromagnetically with one of the orbital electrons of an atom.

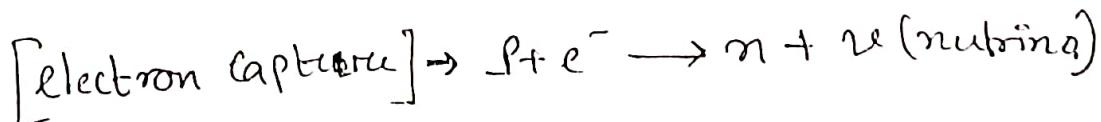
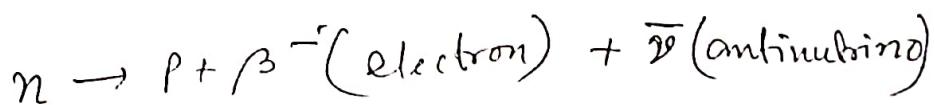
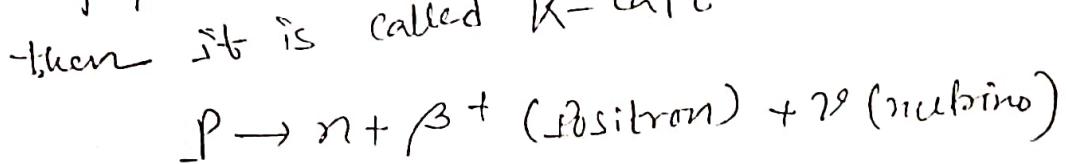
β -Scattering

(i) What do you mean by β -decay / β -disintegration?

(ii) Why β -particle emits from nucleus?

→ (i) Due to instability of nucleus both Positron and electron are emitted from the radioactive nucleus. This phenomenon is known as β -disintegration.

The reverse process is electron capture where the nucleus absorbs one of its own orbital electrons. If the absorption of an electron from the K-shell is called K-capture.

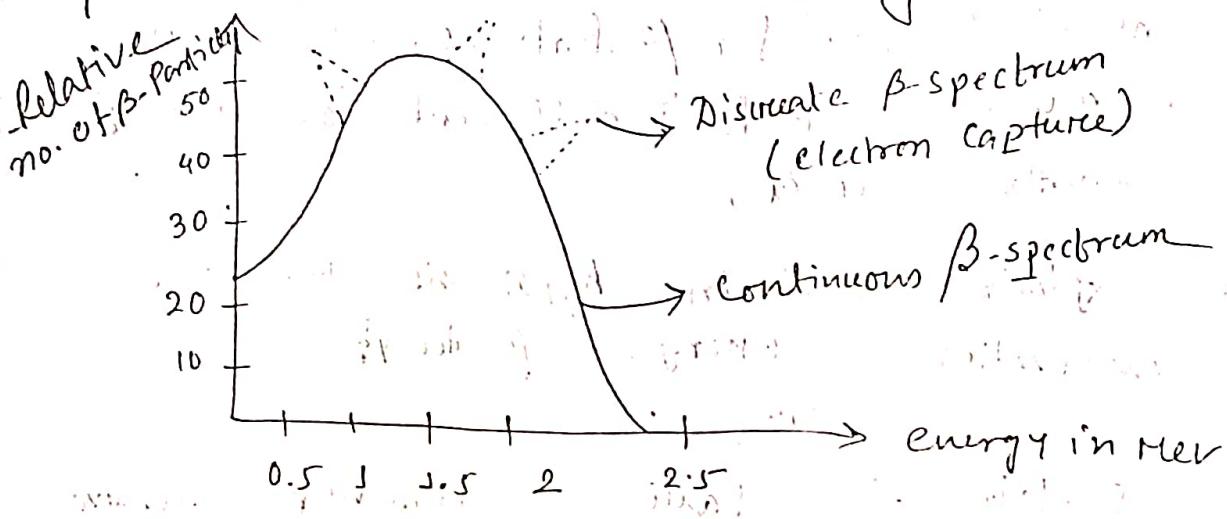


(ii) For the stability of nucleus some time's neutron's are converted to proton and some time's proton's ~~are~~ converted to neutron, when the β -particle (Positron and electron) emits from that nucleus.

(i) Describe the nature of energy spectrum of β -disintegration? write down the importance of β -ray spectrum?

→ the energy of β -Particle's is studied with the help of β -ray spectrometer.

β -ray spectrometer can separate the β -Particle based on different energies of β -Particle by using strong magnetic field. The General distribution of energy in a β -ray Spectrum is shown in the figure:



Characteristic of β -ray Spectrum (Nature)

(i) The β -Spectrum is continuous, having energies ranging from zero to a certain well defined limit known as end point energy (E_m) which is characteristics of the β -emitter.

(ii) The area between the β -spectrum and the energy axis is directly proportional to the number of β -Particles.

(iii) There is a number of sharp lines (Peaks) in the β -spectrum which are found to be very prominent on the photographic plate.

(iv) Every continuous β -spectrum has a definite maximum height and position of which depend on the nucleus emitting the particles.

(v) There is definite upper limit or end point of energy for β -particles, emitted by the nucleus, which is different for different β -emitting nuclei.

Explain Neutrino hypothesis to explain conservation of energy in β decay?

(or)

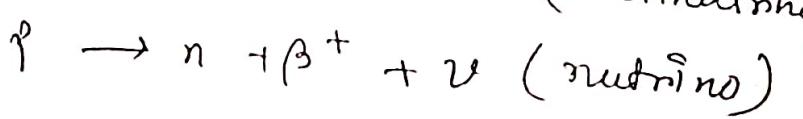
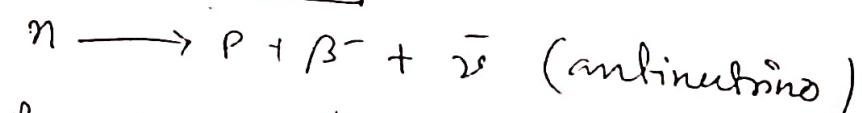
Explain How Pauli's neutrino hypothesis solve the conservation of energy and momentum in β -decay?

→ Pauli's neutrino hypothesis → In neutrino hypothesis it is assumed that, when a nucleus emits a β -particle, a neutron in a nucleus changes to a proton and another particle is also emitted along with β -particle. If only β -particle is emitted from the nucleus, then all the β -particle's for a given radio-sample has same KE. B-cut

actual measurement's show that only few β -Particle's emitted with maximum KE. From β -decay spectrum, the majority of β -Particle emitted with KE in between zero to a maximum value (And Point Energy or Maximum Energy E_{\max}). In this case the conservation of Energy and momentum, do not hold good for single Particle (β^- / β^+).

All this difficulties have been overcome by considering the existence of another type of particle called neutrino, and its anti-particle antineutrino, simultaneously with β Particle. Its existence was first predicted by Pauli on theoretical ground in (1930) and has been experimentally confirmed in 1956. The β -Particle and a neutrino emitted from radioactive nucleus with a const. total energy = ~~different~~ Q value of the reaction, arises from the sharing of total energy between β -Particle and the neutrino. ~~Q~~ value.

$$Q\text{-value} = E_{\beta} + E_n$$



(*) Define thermal neutron?

→ When 1st moving neutron's have been slowed down until the average energy is equal to the 0.03 eV , then the neutron's are called thermal neutron.

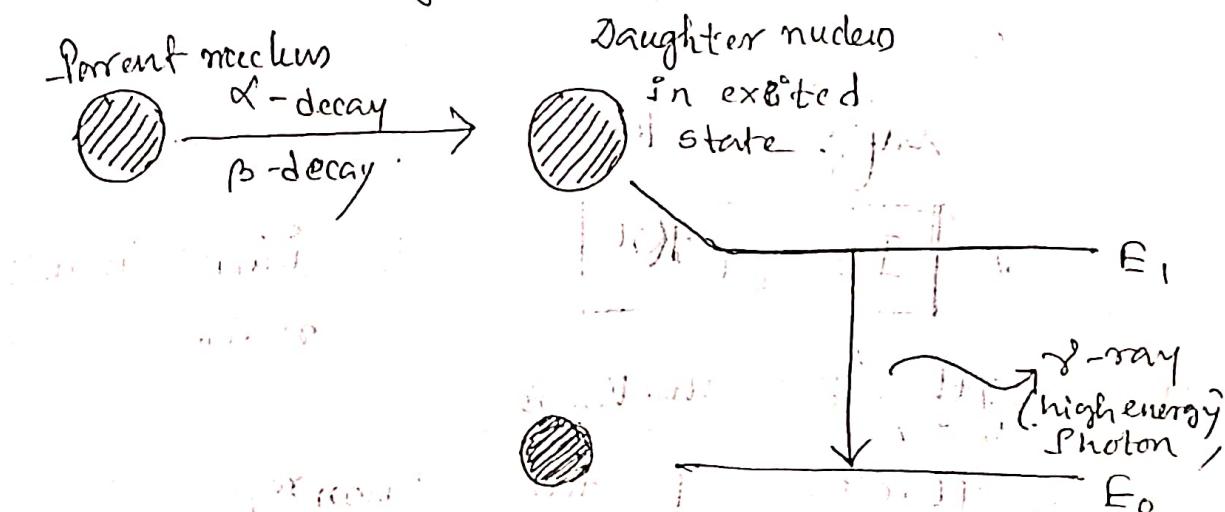
γ -disintegration

(i) How does the intensity of γ -ray changes when it interacts with matter, also defined the term's half-thickness, radiation length/relaxation length?

(ii) Write down the origin of γ -decay?

→ (ii) After β -disintegration or α -disintegration the daughter nucleus may be in higher excited state. But the life time in excited state is very small and the daughter nucleus brought to ground state by emitting a ^{High energy} photon, which is known as γ -decay.

So, γ -decay is followed by α -disintegration and β -disintegration.



ii) While passing through material's gamma photon's are either absorbed or scattered from their path. Due to this, the intensity of γ -ray

is reduced as it passes through the material.

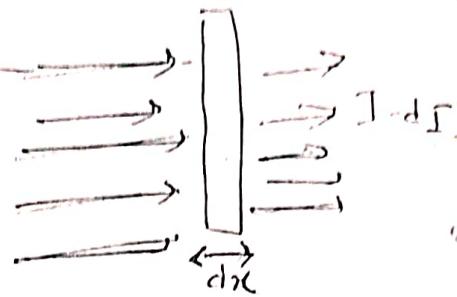
Def:

$I \rightarrow$ Intensity of photon

falling on a

slab of material

of thickness dx .



- the decrease in intensity dI is proportional to initial intensity and thickness dx .

$$\therefore dI \propto I.$$

$$dI \propto n.$$

$$dI \propto -E dx$$

$$\Rightarrow \frac{dI}{I} = -k dx, \mu/k \text{ is proportional const.}$$

Integrating both side w.r.t x ^{= absorption co-effici}
^{proper limit}

$$\int_{I_0}^I \frac{dI}{I} = -k \int_0^x dx$$

$$\Rightarrow \ln\left(\frac{I}{I_0}\right) = -kx$$

$$\Rightarrow \boxed{I = I_0 e^{-kx}}$$

, I_0 = initial intensity

= maximum inten.

Half length / Half thickness :-

- the thickness of the medium required.

- to reduce the intensity to half of the initial value of intensity is known as

Half length / Half thickness.

$$\text{at, } \alpha = y_2, \quad I = \frac{I_0}{2}$$

$$\therefore K \alpha = 0.693$$

$$\Rightarrow \boxed{dy_L = \frac{0.693}{K}}$$

Radiation length / relaxation length :-

The thickness of the medium to require, which reduces the intensity of γ -ray to $\frac{1}{e}$ times of initial intensity, is known radiation length / relaxation length.

at, $\alpha = 1, \quad I = \frac{I_0}{e}$

~~\Rightarrow~~ mention different processes through which γ -rays are absorbed or scattered, by the material.

→ There are mainly three processes through which γ -photon's loss energy, while traveling through the medium.

(i) Photo electric effect :- In photoelectric effect, γ -photon make collision with bound electron of an atom and in this process the whole photon energy is transferred to that electron. If the incident photon energy

is sufficient then, after the collision, the electron is ejected from the atom, which is known as photoelectron.

According to Einstein Photoelectric eqn, the energy of ejected photoelectron is given by.

$$\frac{1}{2}mv_{\max}^2 = h\nu - w_0,$$

$h\nu$ = incident radiation energy

w_0 = work fun

(ii) Compton effect:-

In Compton effect, Photon is scattered by free electron at rest, it is an elastic scattering process in which the incident photon's transferred a portion of its energy to the electron. After the collision, the photon is scattered by an angle ϕ , the electron recoil's at angle θ . In this

Condition KE gained by electron,

$$E = h\nu \left[\frac{\frac{h\nu}{m_0 c^2} (1 - \cos \phi)}{1 + \frac{h\nu}{m_0 c^2} (1 - \cos \phi)} \right]$$

(iii) Pair Production :- In this process γ -photon's with energy greater than 1.02 MeV is converted to pair of electron and positron in presence of highly dense medium (nucleus)

γ -photon $\xrightarrow[\text{medium}]{\text{High Density}}$ electron + Positron
 (e^-) (e^+)

(i) Explain why the minimum energy required for Pair Production is 1.02 MeV .

(ii) Explain why Pair Production is not possible in Vacuum.

→ (i) In Pair Production γ -photon is converted to electron + Positron pair.

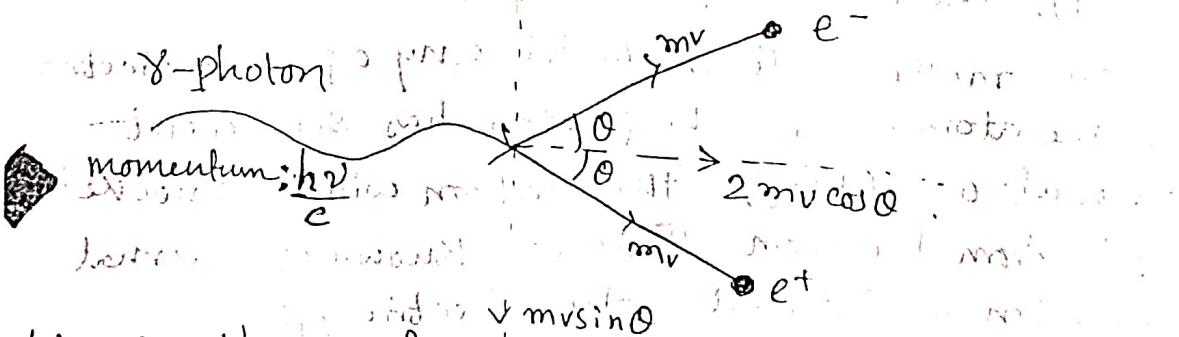
γ -ray \rightarrow electron + Positron

The minimum energy of γ -ray = (e^-) (e^+)

minimum energy of e^- + Rest-mass energy of e^+
 $= m_e c^2 + m_e c^2 = 0.51 \text{ MeV} + 0.51 \text{ MeV}$

That is why minimum energy of γ -photon for

(ii) Pair Production is 1.02 MeV .



We consider a γ -photon with energy $h\nu$.

The momentum of photon = $\frac{h\nu}{c}$

Using momentum conservation along x-axis.

$$\frac{h\nu}{c} = mv \cos \theta + mv \cos \theta$$

$$\Rightarrow h\nu = 2mcv \cos \theta = (2mc^2) \frac{v}{c} \cos \theta$$

\Rightarrow energy of γ -ray = (energy of $e^- + e^+$) $\times \frac{m_e c^2}{c^2}$ $m_e c^2$ = energy of electron/positron.

$$\rightarrow ① \quad 2mc^2 = \text{energy of } e^- + e^+$$

The maximum value of $\cos\theta = 1$ and

γ_c always less than 1.

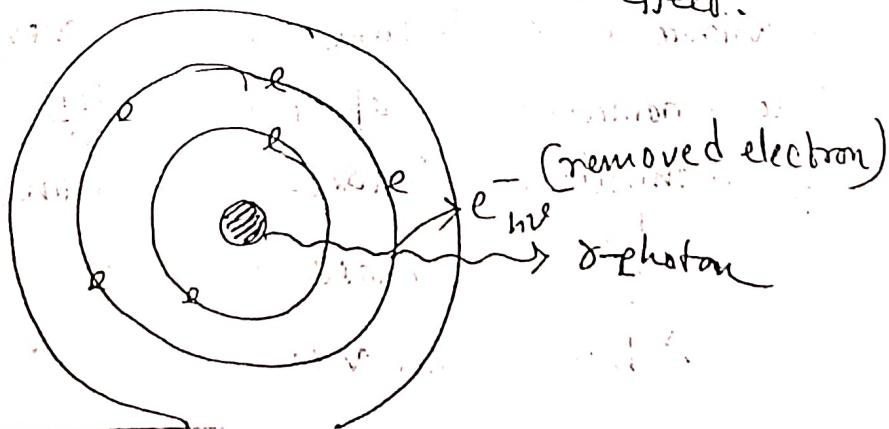
\therefore energy of γ -ray < [energy of $e^- + \text{Positron}(e^+)$]

For any natural process the momentum and mass energy should be consumed simultaneously.

That is why Pair Production is not possible in free Space.

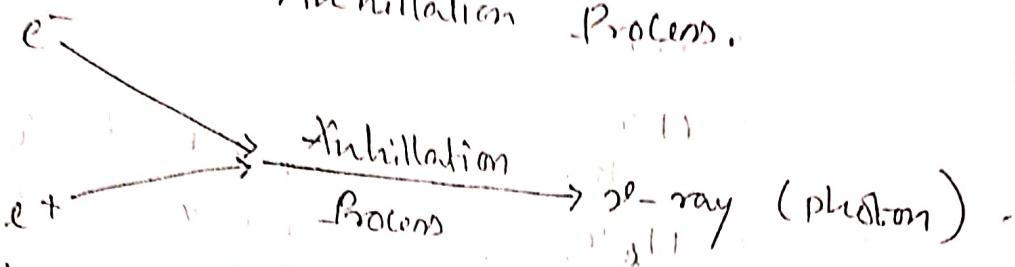
④ What do you mean by internal conversion or internal photoelectric effect.

→ After α -disintegration or β -disintegration the daughter nucleus may be in excited state, but the life time of a nucleus in excited state is very small. When an excited nucleus comes to ground state by emitting high energy photon (γ -ray). There is a possibility that the emitted photon make collision with any of the electron of the atom. If the photon has sufficient amount of energy the electron will be knocked out from the atom. This is known as internal conversion or internal photoelectric effect.



Q) What do you mean by Annihilation Process.

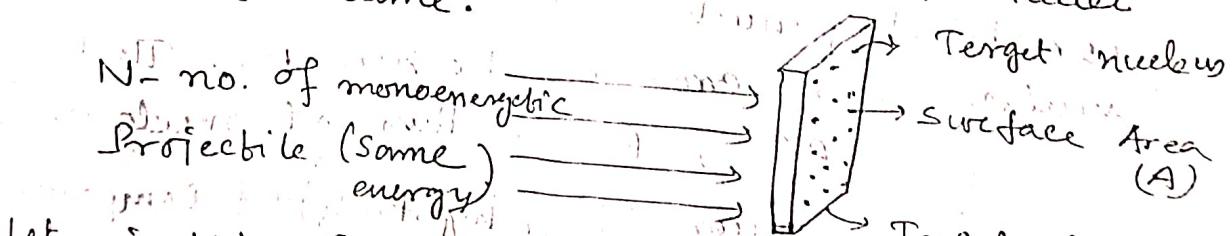
→ When Particle and anti-particle meet with each other they destroy each other's mass and converted the mass into Photon (γ -ray). This Process is known as Annihilation Process.



Q) What do you mean by nuclear cross section. Write down the unit of nuclear cross section.

→ Nuclear reaction cross-section is one of the important parameter in nuclear reaction. It is a quantitative measure of the probability occurrence of a nuclear reaction.

Let a parallel beam of N number of monoenergetic particles be incident per unit time normally on a target foil (containing target nuclei). The surface area of the foil is A and thickness a , having n number of nuclei per unit volume.



Let, in this process ΔN number of nucleus under goes nuclear reaction, ΔN is proportional to

- (i) the intensity of incident projectile.
- (ii) the number of target nuclei in the foil.

$$\Delta N \propto \frac{N}{A} \quad \left[I = \frac{N}{A} = \text{Intensity of projectile} \right]$$

$$\Delta N \propto (A \sigma) n$$

$$\therefore \Delta N \propto n N \sigma n$$

$$\Rightarrow \Delta N = \sigma N n \sigma n$$

$$\Rightarrow \Delta N = \sigma N \frac{n_0}{\text{area}}$$

$$\Rightarrow \Delta N = \sigma N n_0 \frac{n_0}{\text{area}} \quad \left[n_0 = \text{no. of target nuclei per unit area} \right]$$

$$\boxed{\sigma = \frac{\Delta N}{N n_A}}$$

From the above eqn the dimension of σ is [L]⁻²
similar to the dimension of area. This why
 σ is termed as cross-section.

The probability of a nucleate reaction when a single particle ($N=1$) falls on a single target nucleus $\frac{\text{Per}}{\text{Per unit area}} (n_A=1)$, is given by nuclear reaction cross-section,

The unit of nuclear cross-section barn,
 $1 \text{ barn} = 10^{-28} \text{ m}^2$

Geometrically nuclear cross-section equal to two dimension disc area of the nucleus. That is

$$\sigma = \pi R^2, \quad R = \text{radius of nucleus.}$$

④ Explain (Bohr's theory / Bohr hypothesis) of compound nucleus

→ When an incident projectile x enters into a target nucleus A to produce nuclear reaction, a highly excited intermediate state e^*

He found which finally became into the model
and was used another plan like
 $X - K \rightarrow C$
It nucleus X , the practically rapid
capture ν and open other
with no cooling power. But
itself nucleus.

Mining Port in Tiehwa